

# Dynamic Ownership, Private Benefits, and Stock Prices

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## Why should we care?

Controlling shareholders (CS) enjoy private benefits (PB) from holding block of shares

- Social prestige, private amenities, discretion

### Private Benefits affect Stock Prices

#### 1 Size Channel:

PB impact on size of the stake

Amount of shares floating on the market

#### 2 Information Channel:

CS' ownership policy less affected by firm fundamental

CS' ownership policy less informative about firm fundamental

# What I do

## Dynamic model of optimal shareholding

- Heterogeneity between large/small shareholders
- Asymmetric information and private benefits
- Equilibrium ownership policy and stock price

## Structural estimation using

- Time-series of stock prices
- CS' ownership policy



- Quantify PB in terms of equity value
- Measure price impact of PB (counterfactual analysis)

# What I find

## Main Results:

- 1 PB are around 2% of equity value
- 2 CS generally have positive impact on stock prices
- 3 Larger positive impact during 2011-2012
- 4 Larger positive impact with corporations as CS

## Economic Implications:

- (1,2) Extraction of PB no detrimental for residual shareholders
- (3) Beneficial effect of CS during negative cycles
- (1,4) Evidence of synergistic effect

# Literature vs Contribution: Theory

## Ownership Policy of Large Shareholders

- Gomes (2000) (Activism and Asymmetric Information)
- DeMarzo and Urosevic (2006) (Activism and Moral Hazard)
- Collin-Dufresne and Fos (2016) (Activism and Asymmetric Information)

- Heterogeneity large/small shareholders

## ⇒ Persistent Trading by Large Shareholder

! Empirical evidence: frequency of change in stakes of CS

! My model: Asymmetric Information and PB

⇒ Infrequent trading implied by extraction of PB

# Literature vs Contribution: Estimation

## Measuring Private Benefits

- Voting Premium (Voting Share - Non-Voting Share)  
[Zingales (1995), Nenova (2003), Benos and Weisbach (2004)]
- Block Premium (Block price - Market Price)  
[Barclay and Holderness (1989), Nicodano and Sembenelli (2004)]
- Structural Estimation of block pricing model  
[Albuquerque and Schroth (2010)]
- Evidence on Italy  
[Zingales (1995), Nenova (2003),  
Nicodano and Sembenelli (2004), Dyck and Zingales (2004)]

- PB priced in the controlling block acquisition

⇒ **Information on price/size of controlling block purchase**

! PB may impact on the ownership policy

! My approach: model for ownership dynamics of CS

⇒ **Information on CS' ownership policy**

## Literature vs Contribution: Results

- **Price Impact of Private Benefits**

[Lippi and Schivardi (2014)]

→ Counterfactual analysis by model pricing equations ( $PB=0$ )

- **Price Impact of Controlling Shareholders**

[John et al. (2008), Faccio et al. (2011)]

→ Counterfactual analysis by model pricing equations ( $CS=0$ )

- **Stake Valuation by Controlling Shareholders**

[Roger and Schatt (2016), Odegaard (2009)]

→ CS' Certainty Equivalent by model optimality conditions

# The Setup

## Firm Cash-Flows:

$$dD_t = \mu_t dt + \sigma_D dZ_t,$$
$$d\mu_t = \sigma d\tilde{Z}_t,$$

## Firm Shareholders:

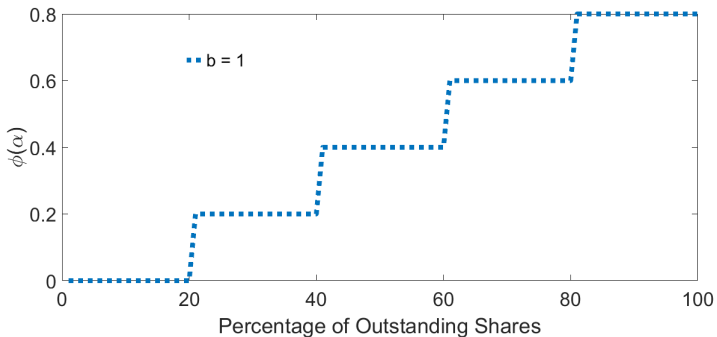
- Continuum of (risk-averse) Marginal Investors (MI)
  - MI have heterogenous prior on  $\mu_t$
  - Continuous trading on their priors
  - Bayesian update on  $\mu_t$
- One Large (risk-averse) Shareholder (CS)
  - Perfect knowledge on  $\mu_t$
  - May trade at discrete dates  $\tau$
  - Extracts PB from stake accruing to total wealth



# Private Benefits Function

$$\phi(\alpha) = b * \alpha_j,$$

if  $\alpha_j \leq \alpha < \alpha_{j+1}$



# Investors learning

Marginal investors learn about  $\mu_t$  (Bayesian heterogenous update)

- Continuous common (noisy) signal  $dD_t = \mu_t dt + \sigma_D dZ_t$

$$\bar{\mu}_{t+dt} = (1 - \bar{k}_t)\bar{\mu}_t + \bar{k}_t dD_t$$

$\bar{k}_t$  = average reaction to the new signal

▶ Proof1

- Discrete common (noisy) signal  $\alpha_{L,\tau}$

$$\bar{\mu}_\tau = \bar{\mu}_{t < \tau} + \bar{g}(\alpha_{L,\tau} - \alpha_{L,\tau}(\bar{\mu}_{t < \tau}))$$

$\bar{g}$  = average reaction to the CS' ownership policy

▶ Proof2

# Model Equilibrium

- **Optimality Condition of CS** (Share Benefits = Total Cost of a Share)

$$V' = P_\tau + (\alpha_{L,\tau} - \alpha_{L,\tau^-})P'$$

$V$  = Present value of net benefits flow

**Net benefits** = Risk-adjusted dividends + private benefits

- **Equilibrium Stock Price**

$$P_\tau = \int_\tau^\infty e^{-r(s-\tau)} \left[ \underbrace{\bar{\mu}_\tau}_{\text{Information Channel}} - \underbrace{\rho_\tau}_{\text{Size Channel}} \right] ds,$$

$$\rho_\tau = (1 - \alpha_{L,\tau})a^I \sigma_D^2 r$$

▶ Proof3

# Model Results

## Asymmetric Information and No PB

- CS always tempted to trade on mispricing of MI
- MI learn from CS' trading
- CS (always) trades (gradually) towards optimal risk-sharing allocation  
[equivalent to DeMarzo and Urosevic (2006)]

## Asymmetric Information and PB

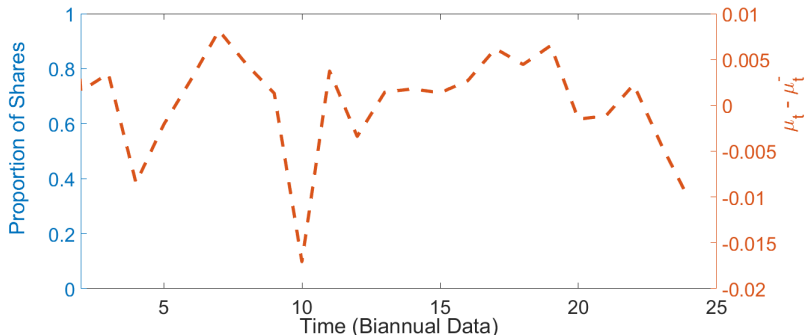
- CS only trades when mispricing is large enough

**Buys** → Gain in PB offsets (total) trading costs

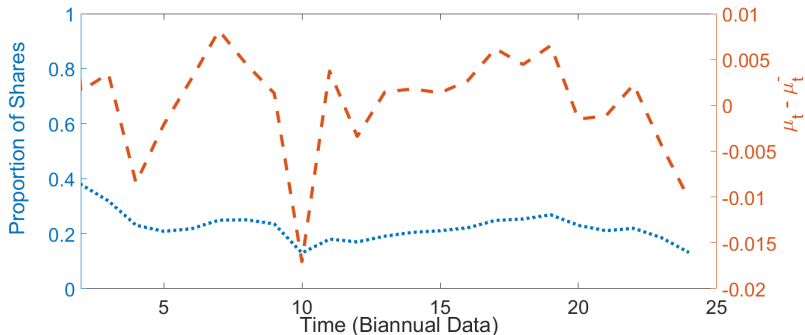
**Sells** → Loss in PB offsets (net) trading gains

## AI and No PB: Mispricing

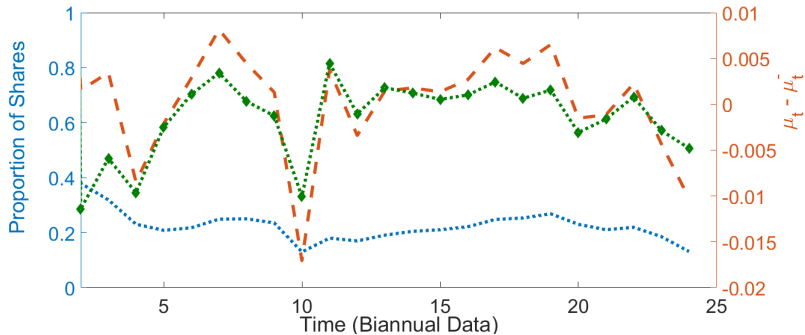
▶ Numerical Setup

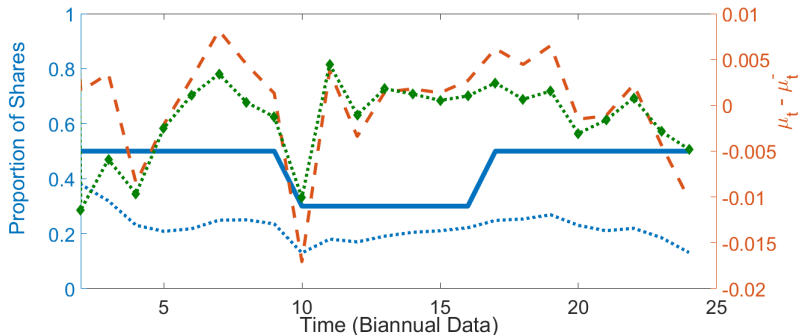


## AI and No PB: Ownership policy



## AI and No PB: Learning



AI and PB: Ownership Policy ▶ Updating Weight



# Data

Public companies listed in Italian Stock Exchange (Non-financial firms) (2004-2016)

- Ownership Stake of Controlling Shareholder (Biannual, TR + CONSOB)
- Stock Prices (Daily and Biannual, Datastream)
- Earnings-per-Share (Annual, Datastream)

Sample Selection

- Same Largest Shareholder for  $\geq 75\%$  of observations
- Complete Time-Series on all data
- Final Sample: 77 Firms
- CS' type: 34 Corp, 30 Ind, 10 Gov, 3 Fin

Variable	Mean	Median	STD	p10	p90
Stake Level (%)	48.63	53.29	17.53	18.88	66.96
N of Trades	3.33	3	2.34	1	6
Daily Turnover	0.38	0.23	0.60	0.02	5.26
Stake Change (%)	4.27	1.17	0.41	0.00	4.35

## Ownership Policy: Empirical Facts

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- When they do, they trade big blocks of shares
  - The mean (median) change in stake is 4.27% (1.17%)

## Ownership Policy: Empirical Facts

- CS change their stakes infrequently
  - Change in stake observed in 18% of total observations
- When they do, they trade big blocks of shares
  - The mean (median) change in stake is 4.27% (1.17%)
- They rarely trade small blocks
  - Change  $< 1\%$  observed in 7.79% of total observations

# Estimation Problem

For each firm:

## Quantities to estimate:

- Model Parameters

$$\theta = \{\sigma_D, \sigma, a^L, \bar{g}(0), \sigma_\epsilon^2, b\}$$

- Latent Variables

$$X_t = \{\mu_t, \bar{\mu}_t\}$$

## Observable Variables:

- Daily Stock Prices
- Biannual Stock Prices
- Biannual Stakes
- Annual Earnings-per-Share

## Equilibrium Conditions:

- Market Clearing
- Equilibrium Stock Price
- Optimality of CS

# First Step: $\{\sigma_D, \sigma, \mu_t, \bar{\mu}_t\}$

- **State Diffusion:** from market clearing  $\int_i d\alpha_{i,t} = 0$ ,

$$E_t[\bar{\mu}_{t+1}] = (1 - \bar{k})\bar{\mu}_t + \bar{k}\mu_t,$$

$$E_t[\mu_{t+1}] = \mu_t$$

- **Observable Equation:** Stock Price

$$P_t = [-(\sigma_D^2 a^I r(1 - \alpha_{L,t})) + \bar{\mu}_t]/r$$

- **Additional Restriction:** from FCF dynamics

$$\text{var}(\delta(dD_t)) = \text{var}(\delta(d\mu_t)) + 2\text{var}(dD_t - \mu_t) = \sigma^2 + 2\sigma_D^2$$

⇒ **Kalman Filter**, with daily stock prices

- Predict  $P_t$  with prior on  $X_t = \{\mu_t, \bar{\mu}_t\}$
- Obtain prediction error using actual prices
- Update  $X_t$  based on prediction error ⇒ Maximum Likelihood on the errors

$$e_t = e(a^I, \sigma, \sigma_D, X_t)$$

## Second Step: $\{a^L, \bar{g}(0), \sigma_\epsilon^2\}$

One equation for stock price at  $\tau$  (disclosure dates),

$$P_\tau = [-(\sigma_D^2 a^I r(1 - \alpha_{L,\tau})) + \bar{\mu}_\tau]/r,$$

by eliminating all the remaining endogenous quantities, only function of

- Stake of CS:  $\{\alpha_{L,\tau}\}$
- Exogenous variables:  $\{a_L, \bar{g}(0), \sigma_\epsilon^2\}$

⇒ **Kalman Filter**, with biannual stock prices

- Predict  $P_\tau$  using  $\bar{\mu}_\tau$
- Obtain prediction errors using actual prices ⇒ Maximum Likelihood on the errors

$$e_\tau = e(a_L, \bar{g}(0), \sigma_\epsilon^2, \bar{\mu}_\tau)$$

Identification:  $b$ Lower and Upper bounds for  $b$ 

The actual choice  $\alpha_{L,\tau}$  is not optimal without PB

⇒ Without private benefits CS chooses  $\alpha_{m,\tau}$

## Lower Bound

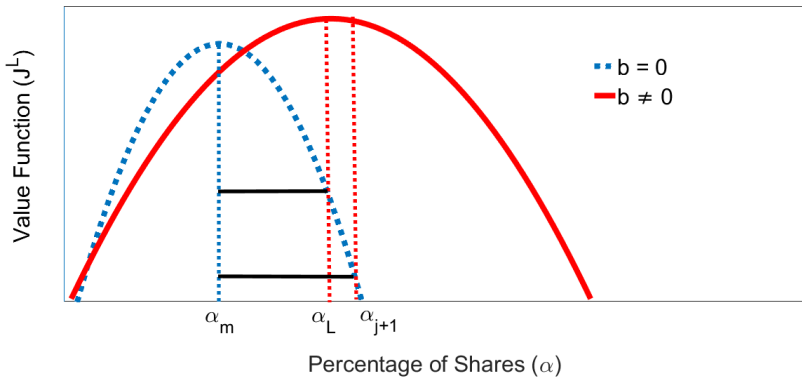
The gain in PB must be at least equal to the loss in the marginal utility

Why does not the CS jump to higher thresholds?

## Upper Bound

PB are not sufficient to jump to higher threshold given loss in marginal utility



Identification:  $b$ 

# Measuring Price Impact

## Counterfactual Analysis:

- 1 Stock Price without PB:  $\{P_\tau^m\}$
- 2 Stock Price without CS :  $\{P_\tau^n\}$

$$P_\tau^m = P \left( \alpha_{L,\tau} = \alpha_{m,\tau}, \bar{\mu}_\tau = \bar{\mu}(\alpha_{m,\tau}), \sigma_\epsilon^2 = 0 \right),$$

$$P_\tau^n = P \left( \alpha_{L,\tau} = 0, \bar{\mu}_\tau = \bar{\mu}_{t < \tau} \right),$$

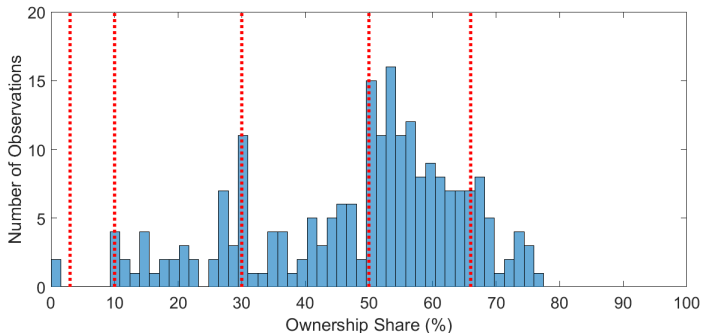
### Price Impact

$$\psi^m = \frac{P_\tau - P_\tau^m}{P_\tau^m},$$

$$\psi^n = \frac{P_\tau - P_\tau^n}{P_\tau^n},$$

## PB thresholds

Ownership Share	Right/Commitment
3%	Obligation to stake disclosure
10%	Right to call shareholders meeting
30%	Obligation to launch takeover
50%	Company control
66%	Right to call extraordinary meeting

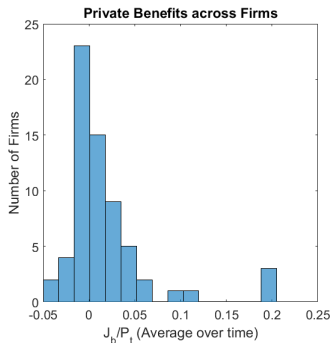
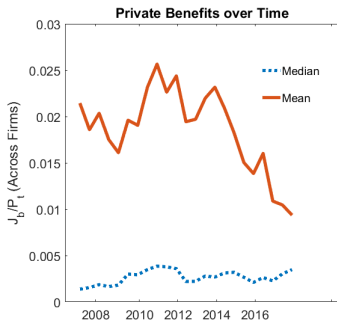


## Model Fit

	Mean	Median	Std	10th pct	90th pct
$\sigma$	0.024	0.016	0.028	0.002	0.051
$\sigma_D$	0.279	0.210	0.294	0.038	0.639
$a_L$	2.664	2.137	1.452	1.131	4.999
$b$	0.001	0.000	0.008	-0.003	0.009
$\bar{g}(0)$	0.137	0.041	0.172	0.000	0.493
$\sigma_\epsilon^2$	0.584	0.764	0.405	0.000	0.998
	Mean		Median		
	Actual	Fitted	Actual	Fitted	
Stock Price volatility	1.98	2.05	1.22	1.19	
CS' Trading volatility	0.029	0.031	0.016	0.014	
Trade (% of shares)	7.73	11.73	3.64	5.46	
	Actual	Fitted			
N of Trades $\geq 1\%$	10.76%	6.63%			

- Good performance in replicating features of data
- Prediction of larger blocks trades, with lower frequency

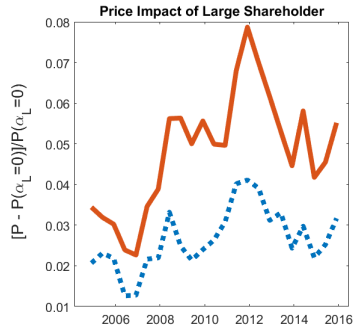
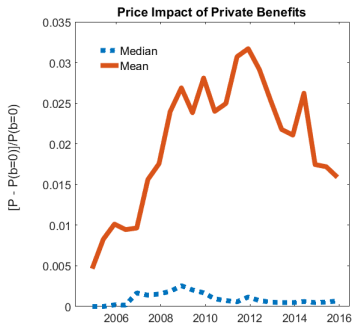
# Private Benefits



- PB around 2% of equity value
- Positive skewness in distribution of PB
- 50% of CS extract PB < 1% of equity

▶ Table

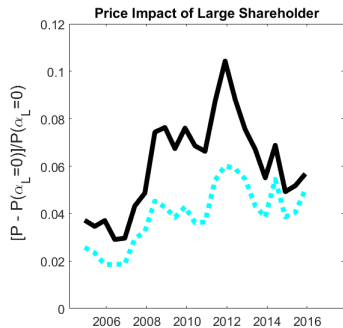
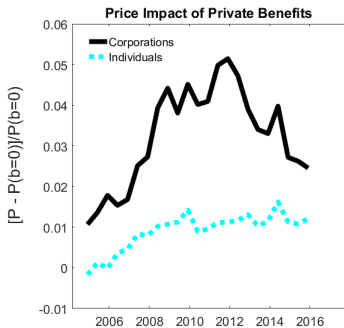
# Price Impact



- General positive impact on stock prices
- Heterogeneity and positive skewness
- Larger during 2011-2012 crisis

▶ Table

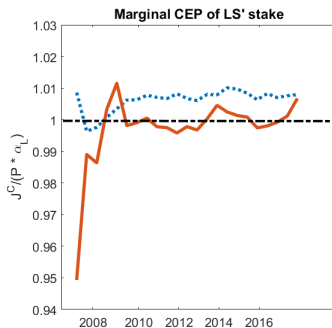
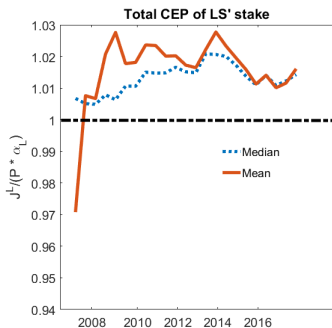
# Type of CS



- Larger impact with corporations as CS

▶ Table

# Certainty Equivalent



- Valuation of a share out of market price
- Not observable without trade

► Table



## Implications & Conclusion

- Dynamic model of optimal shareholding (AI and PB)
- Model restrictions to
  - **Quantify PB of Controlling Shareholders**
  - **Measure the price impact of PB and CS**

**Beneficial effect of CS for residual shareholders**  
[Negative Cycles and Corporations]

# Estimation Results

▶ back3

Table: . Private Benefits and Stock Price

Panel A: All Sample				
	Mean	Median	10th pct	90th pct
$J^L/P$	1.015	1.014	0.984	1.053
$J_b/P$	0.018	0.003	-0.015	0.054
$J_C/P$	0.997	1.006	0.945	1.054
$\psi^m$	0.020	0.002	-0.021	0.096
$\psi^n$	0.048	0.028	-0.001	0.128
Panel B: Corporations				
	Mean	Median	10th pct	90th pct
$J^L/P$	1.018	1.022	0.982	1.063
$J_b/P$	0.029	0.009	-0.016	0.105
$J_C/P$	0.989	1.002	0.865	1.052
$\psi^m$	0.032	0.003	-0.018	0.127
$\psi^n$	0.060	0.046	0.001	0.149
Panel C: Individuals				
	Mean	Median	10th pct	90th pct
$J^L/P$	1.013	1.014	1.001	1.023
$J_b/P$	0.011	0.001	-0.010	0.011
$J_C/P$	1.002	1.007	0.967	1.059
$\psi^m$	0.009	0.002	-0.026	0.029
$\psi^n$	0.039	0.021	-0.002	0.132

# Numerical Simulations

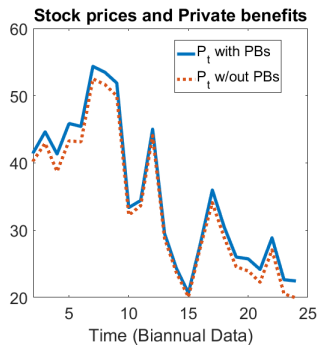
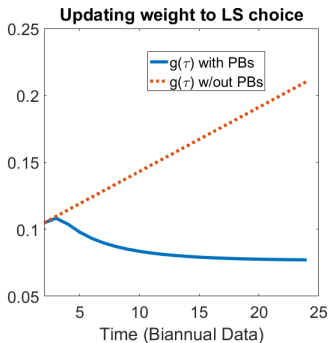
▶ [back1](#)

Table: . Parameters Estimates: Simulation Study

	True	Mean	Median	10th pct	90th pct
$\sigma$	0.1	0.093	0.093	0.087	0.099
$\sigma_D$	0.2	0.202	0.199	0.132	0.274
$a_L$	8	8.71	7.97	7.10	10.36
$b$	0.02	0.019	0.021	0.007	0.027
$\bar{g}(0)$	0.1	0.097	0.099	0.082	0.105
$\sigma_\epsilon^2$	0.2	0.189	0.188	0.138	0.245

# Noise and Impact

▶ back2



## Proof 1

$$\alpha_{i,t} = \frac{\mu_{i,t} - \bar{\mu}_t + \rho}{ar\sigma^2}, \rho_t = (1 - \alpha_{L,t})a^I r\sigma^2$$

$$d\alpha_{i,t} = \frac{1}{ar\sigma^2}(d\mu_{i,t} - d\bar{\mu}_t)$$

$$d\mu_{i,t} = k_i\eta_{i,t}, k_i = \frac{\sigma_i^2}{\sigma_D^2 + \sigma_i^2},$$

$$\eta_{i,t} = dD_t - E_{i,t}[dD_t], E_{i,t}[dD_t] = \mu_{i,t}$$

Since,

$$\int_i d\alpha_{i,t} = 0$$

$$\int_i d\mu_{i,t} di = Md\mu_t \rightarrow d\mu_t = \frac{1}{M} \int_i (k_i(dD_t - E_{i,t}(dD_t))) = \bar{k}(dD_t - \mu_t)$$

► Investors Learning

## Proof 2

$$d\alpha_{i,\tau} = \frac{1}{ar\sigma^2}(d\mu_{i,\tau} - d\bar{\mu}_\tau)$$

$$d\mu_{i,\tau} = g_i(\tau^-)(\alpha_{L,\tau} - E_{t<\tau}(\alpha_{L,\tau})), d\bar{\mu}_\tau = \bar{\mu}_\tau - \bar{\mu}_{t<\tau}$$

Since,

$$\int_i d\alpha_{i,\tau} = 0 \rightarrow \int_i d\mu_{i,\tau} di = Md\bar{\mu}_\tau$$

$$d\bar{\mu}_\tau = \frac{1}{M} \int_i (g_i(\alpha_{L,\tau} - E_{t<\tau}(\alpha_{L,\tau}))) di = \bar{g}(\tau^-)(\alpha_{L,\tau} - E_{t<\tau}(\alpha_{L,\tau}))$$

$$\alpha_{L,\tau} = \frac{\mu_t - \bar{\mu}_\tau + (1 + \alpha_{L,\tau^-})a^I\sigma_D^2 r + \phi(\alpha_{L,\tau})}{2a^I\sigma_D^2 r + a^L\sigma_D^2 r}$$

$$E_{t<\tau}(\alpha_{L,\tau}) = \frac{(1 + \alpha_{L,\tau^-})a^I\sigma_D^2 r}{2a^I\sigma_D^2 r + a^L\sigma_D^2 r}$$

$$g_i(\tau^-) = \frac{\alpha_{L,\tau^-}^\mu \sigma_i^2}{(\alpha_{L,\tau^-}^\mu)^2 \sigma_i^2 + \sigma_\epsilon^2}, \alpha_{L,\tau}^\mu = \frac{\partial \alpha_{L,\tau}}{\partial \mu_t}$$

## Proof 3

CEP

$$\frac{\alpha_{i,\tau}\mu_{i,\tau} - \frac{1}{2}\alpha_{i,\tau}^2 a^i \sigma_D^2 r}{r}$$

CEP = cost of share

$$\frac{\alpha_{i,\tau}\mu_{i,\tau} - \frac{1}{2}\alpha_{i,\tau}^2 a^i \sigma_D^2 r}{r} = \alpha_{i,\tau} P_\tau$$

$$\alpha_{i,\tau} = \frac{\mu_{i,\tau} - r P_\tau}{a r \sigma^2}$$

Since,

$$\int_i \alpha_{i,\tau} = (1 - \alpha_{L,\tau})$$

Substitute  $\alpha_{i,\tau}$  and solve for  $P_\tau$ 

$$P_\tau = \frac{\bar{\mu}_\tau - (1 - \alpha_{L,\tau}) * a^I \sigma_D^2 r}{r},$$

where  $\bar{\mu}_\tau = \int_i \mu_{i,\tau} di$ 

▶ Model Equilibrium